



# Parallelising the Monte Carlo simulation of THz conductivity

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# Outline

***1. THz conductivity in nanomaterials***

***2. Parallelization of the algorithm***

- *Integration algorithms*
- *Spatial / Temporal parallelisation*

***3. Achieved results***

***4. Summary and areas to improve***



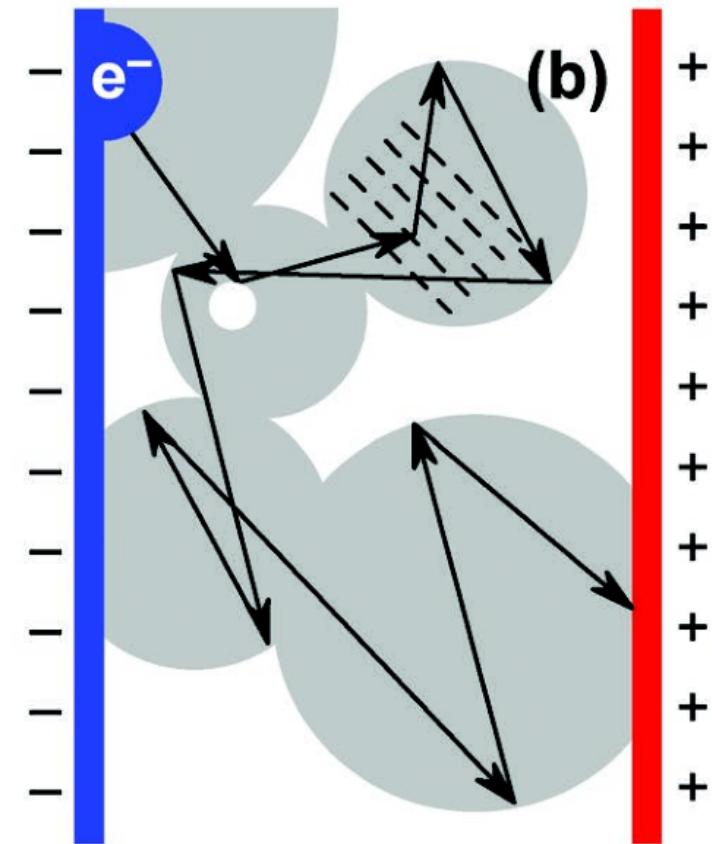
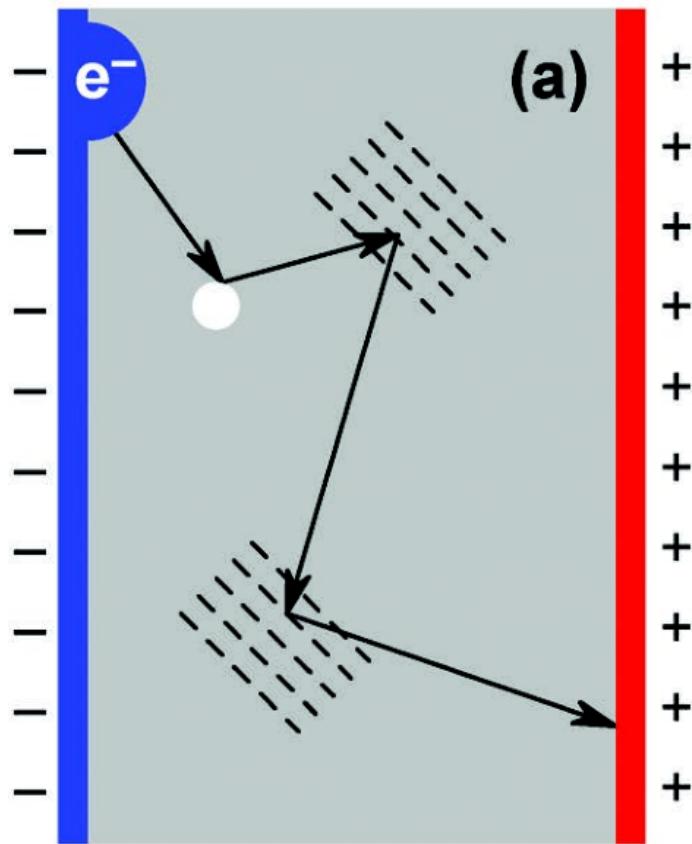
# THz conductivity

*Wide range of applications:*

- *Transparent electrodes in displays and solar cells*
- *Quantum Dots*
- *Nanocomposites*
- *Spectroscopy*
- *... the list goes on*



# Simulation algorithm



# Simulation algorithm

$$\sigma(\omega) = \sigma_1(\omega) + \sigma_2(\omega) = \frac{\sum_{k=\overline{1,M}} \langle v_y(0), v_y(t_k) \rangle e^{i\omega t_k}}{\sum_{l=\overline{1,M}} \cos \omega t_l e^{i\omega t_l}}$$



# Integration methods

- 1. Forward Euler and Backward Euler***
- 2. Runge–Kutta 4***
- 3. Velocity Verlet***
- 4. Leapfrog***



# Naïve spatial parallelisation — OpenMP

## **Pros:**

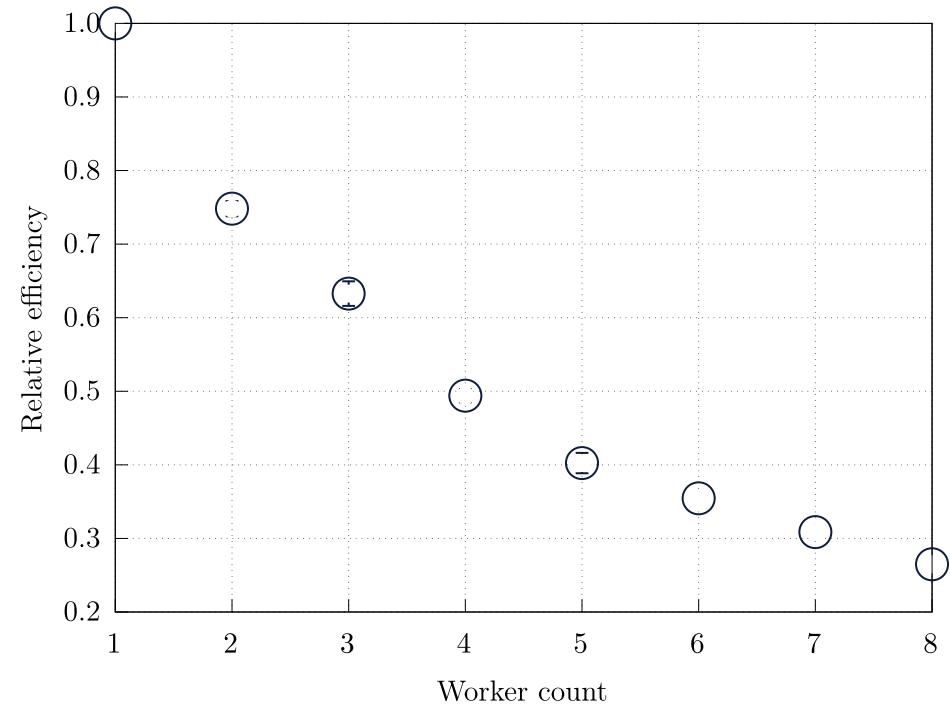
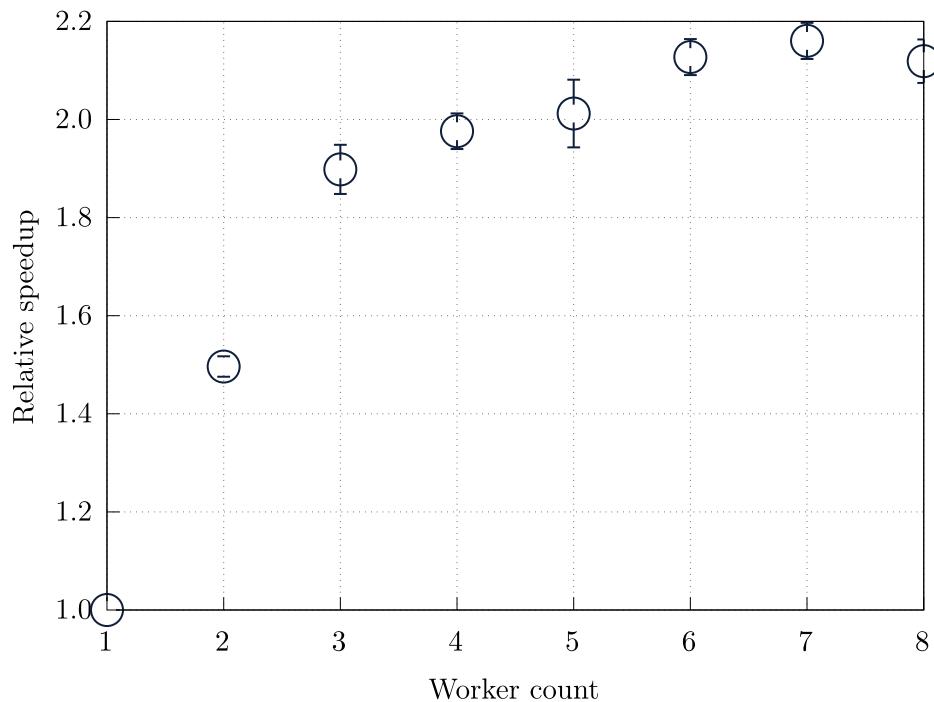
- ***Ease of transition from serial to parallel***
- ***Wide compiler support for* `omp #pragmas`**

## **Cons:**

- ***Codegen causes difficult debugging***
- ***Less robust than solutions like MPI***

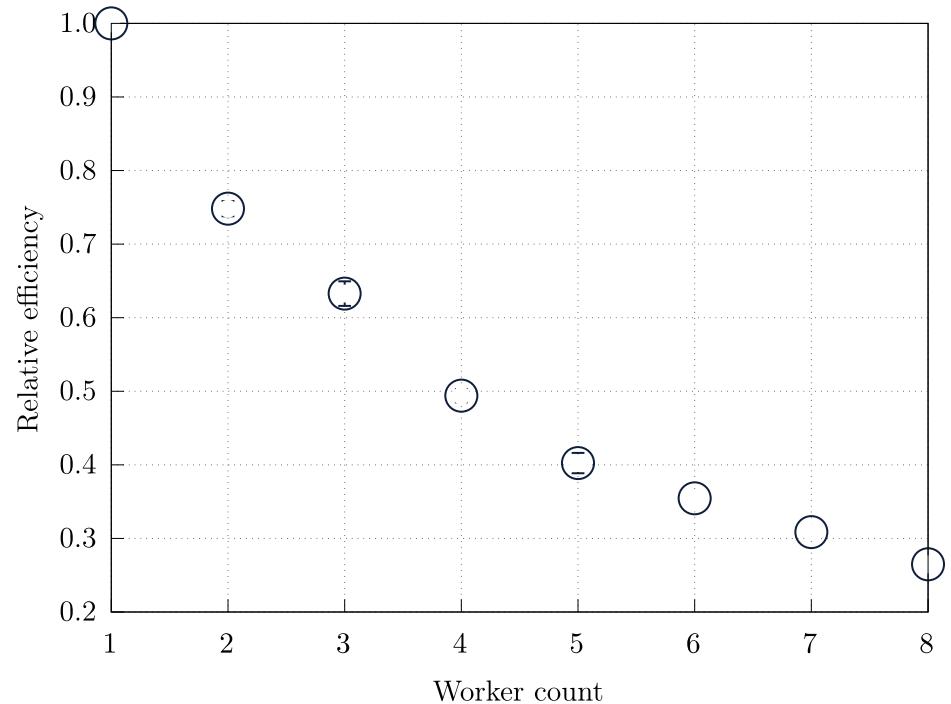


# Results

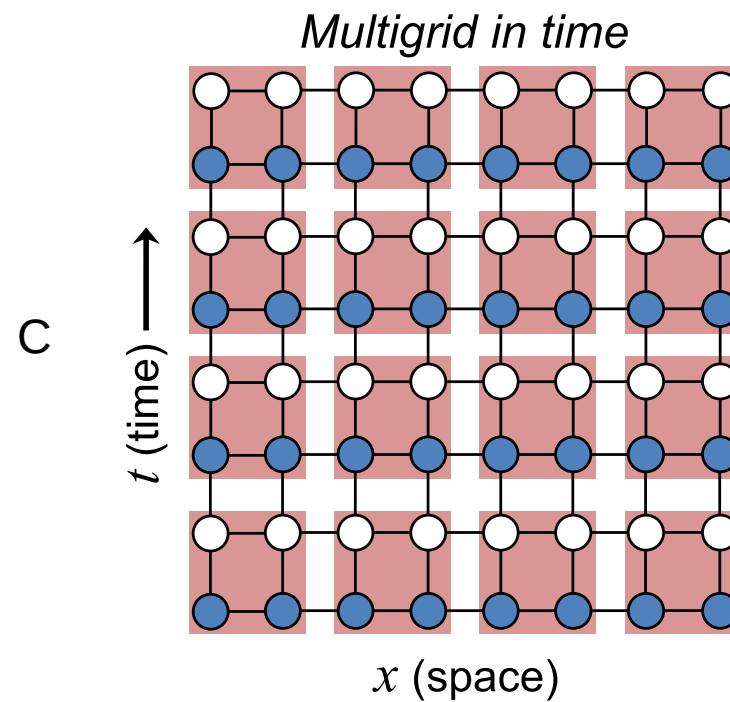
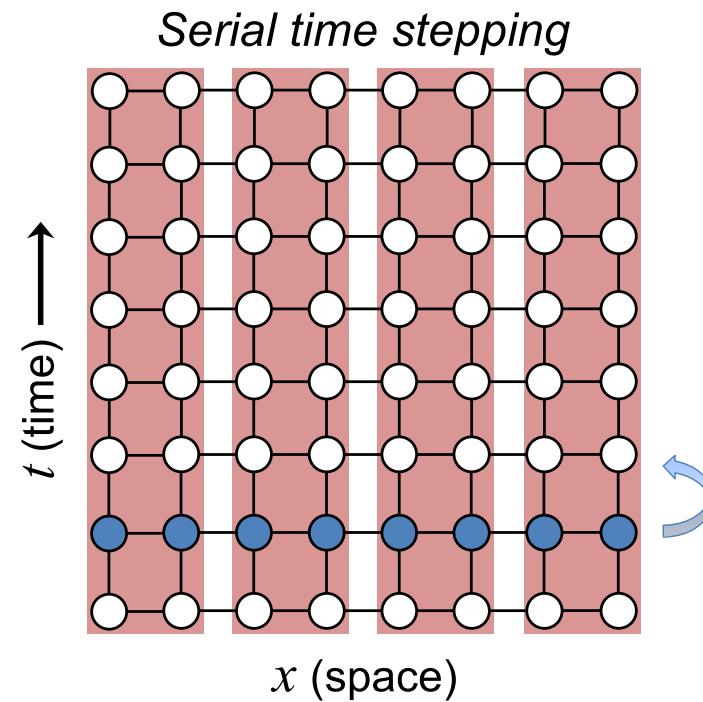


# Results

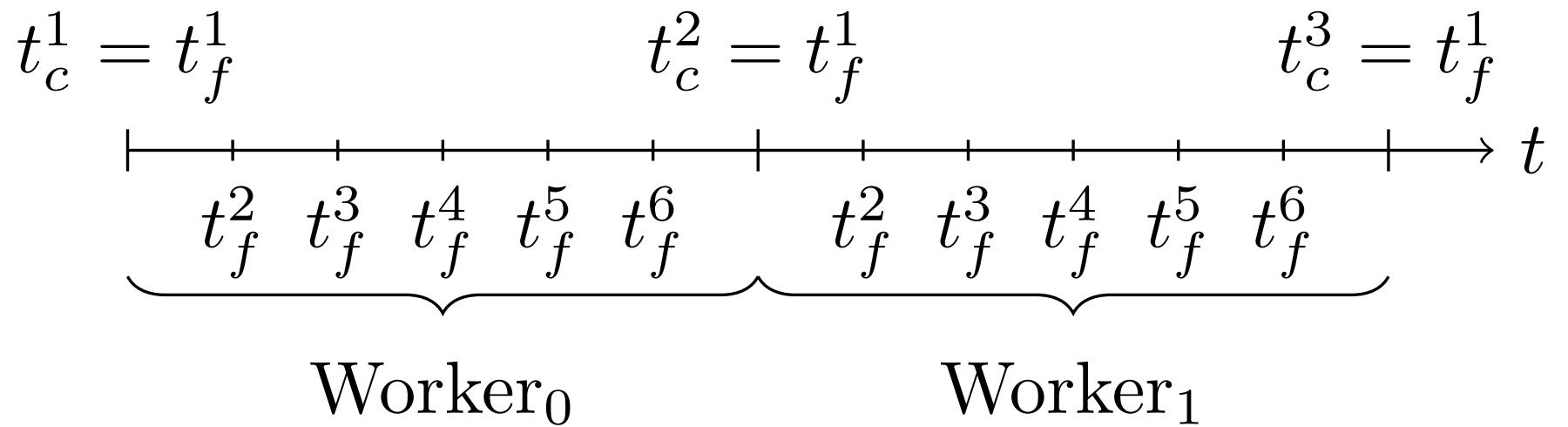
*Time integration  
becomes the  
bottleneck*



# Eliminating the bottleneck — MGRIT



# Temporal parallelisation — MGRIT



# Temporal parallelisation — MGRIT

- *Xbraid*
- C/C++
- «*Black box*» API



# Acknowledgement

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- Vladislava V. **Bulgakova**
- Pavel A. **Chizhov**
- Alexander A. **Ushakov**

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